

Block: _____

Name: Practice Test

Chapter 6 Test – Linear Equations

Version P

/25

Learning Outcomes	Can Start		Can Partially		Can Do	
1. Can solve linear systems using elimination and substitution						
2. Can solve linear inequalities by graphing them.						
3. Can solve a system of linear inequalities.						
4. Can solve linear inequalities applications in context.						
5. Can optimize the solution to linear inequalities by creating an objective function.						
TEST SCORE	0	1	2	3	4	5

Show all of your work.

PART 1:	Can Start		Can Partially		Can Do	
Can solve linear systems using elimination and substitution						

1. Solve the system by the **elimination** method.

$$\begin{array}{r}
 (x + 4y = 2) \times -2 \\
 2x + 5y = -2 \\
 + \quad -2x - 8y = -4 \\
 \hline
 -3y = -6 \\
 \quad \quad -3 \\
 \hline
 y = 2
 \end{array}$$

$$\begin{array}{r}
 x + 4y = 2 \\
 x + 4(2) = 2 \\
 x + 8 = 2 \\
 \quad \quad -8 \quad -8 \\
 \hline
 x = -6
 \end{array}$$

-6, 2

check: $-6 + 4(2) = 2$
 $-6 + 8 = 2$
 $2 = 2 \checkmark$

2. Solve the system by the **substitution** method.

$$\begin{array}{r}
 -4x \quad \quad -4x \\
 4x - 3y = 10 \longrightarrow -3y = -4x + 10 \longrightarrow y = \frac{4}{3}x - \frac{10}{3} \\
 3x + 5y = -7
 \end{array}$$

check: $4(1) - 3(-2) = 10$
 $4 + 6 = 10$
 $10 = 10 \checkmark$

$$\begin{array}{r}
 3x + 5\left(\frac{4}{3}x - \frac{10}{3}\right) = -7 \\
 \left(3x + \frac{20}{3}x - \frac{50}{3} = -7\right) \times 3 \\
 9x + 20x - 50 = -21 \\
 29x - 50 = -21 \\
 \quad \quad +50 \quad +50 \\
 \hline
 29x = 29 \\
 \frac{29x}{29} = \frac{29}{29} \\
 x = 1
 \end{array}$$

$$\begin{array}{r}
 y = \frac{4}{3}(1) - \frac{10}{3} \\
 y = \frac{4}{3} - \frac{10}{3} \\
 y = \frac{-6}{3} \\
 y = -2
 \end{array}$$

1, -2

3. Solve the system using a **method of your choice**.

$$\begin{array}{r}
 +\frac{3}{4}y \quad \quad +\frac{3}{4}y \\
 x - \frac{3}{4}y = \frac{1}{4} \\
 \left(\frac{5}{3}x - 3y = -\frac{4}{3}\right) \times 3 \longrightarrow 5x - 9y = -4
 \end{array}$$

$$\begin{array}{r}
 x = \frac{3}{4}y + \frac{1}{4} \\
 5\left(\frac{3}{4}y + \frac{1}{4}\right) - 9y = -4 \\
 \left(\frac{15y}{4} + \frac{5}{4} - 9y = -4\right) \times 4 \\
 15y + 5 - 36y = -16 \\
 \quad \quad -5 \quad \quad -5 \\
 \hline
 -21y = -21 \\
 \quad \quad -21 \quad -21 \\
 \hline
 y = 1
 \end{array}$$

$$\begin{array}{r}
 x = \frac{3}{4}(1) + \frac{1}{4} \\
 x = \frac{3}{4} + \frac{1}{4} \\
 x = 1
 \end{array}$$

check:
 $\frac{5}{3}(1) - 3(1) = -\frac{4}{3}$
 $\frac{5}{3} - 3 = -\frac{4}{3}$
 $\frac{5}{3} - \frac{9}{3} = -\frac{4}{3}$
 $-\frac{4}{3} = -\frac{4}{3} \checkmark$

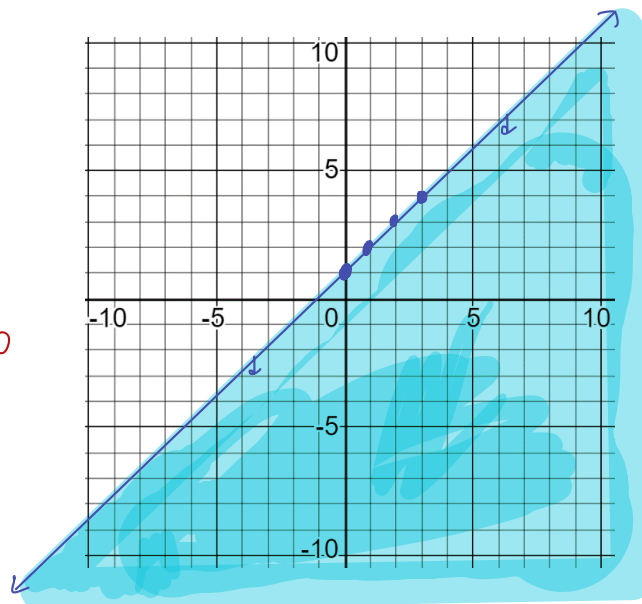
1, 1

PART 2:	Can Start		Can Partially		Can Do	
Can solve linear inequalities by graphing them.						

1) Solve the inequality by graphing: $-x + y \leq 1$

$$y \leq x + 1$$

$b = 1$
 $m = 1$
 • shade below
 • solid line



2) Solve the inequality by graphing: $4x - 5y < 10$

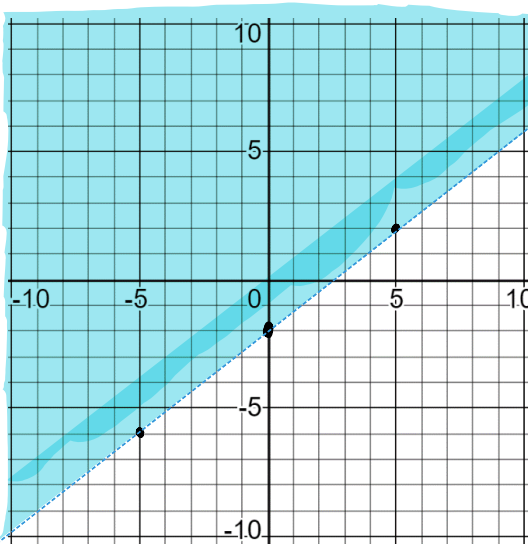
$$4x - 5y < 10$$

$-4x$ $-4x$

$$\frac{-5y < -4x + 10}{-5}$$

$$y > \frac{4}{5}x - 2$$

- dotted line
- Shade above



PART 3:	Can Start		Can Partially		Can Do	
Can solve a system of linear inequalities.						

3) Solve the system of inequalities by graphing:

$$2x - 3y \leq 6 \longrightarrow \begin{array}{l} 2x - 3y \leq 6 \\ \quad \quad \quad -2x \\ \hline \end{array}$$

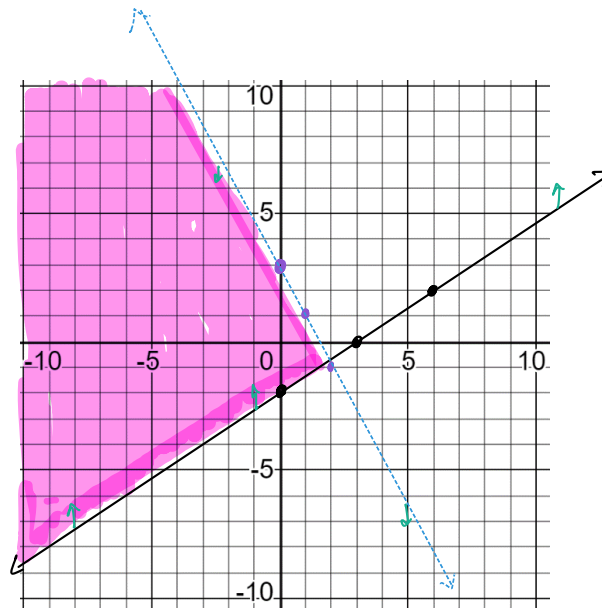
$$y < -2x + 3$$

- dotted line
- shade below

$$\begin{array}{l} -3y \leq -2x + 6 \\ \quad \quad \quad \quad \quad -3 \\ \hline \end{array}$$

$$y \geq \frac{2}{3}x - 2$$

- solid line
- shade above



4) Solve the system of inequalities by graphing:

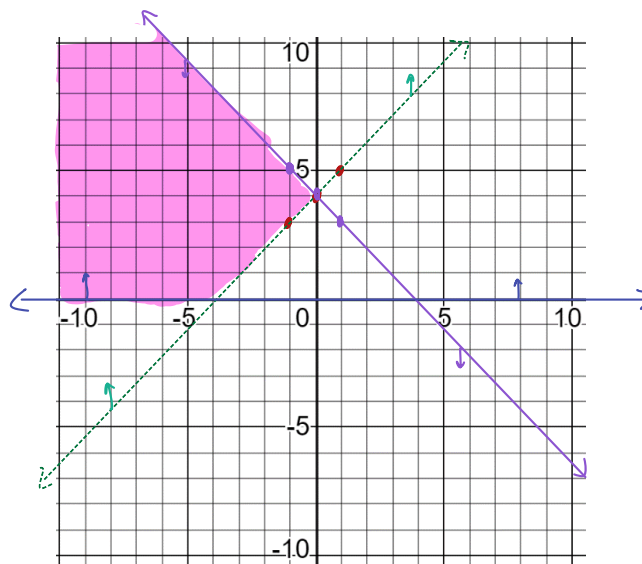
$$\begin{array}{l} -x \\ +y \end{array} \leq 4$$

$$y \leq -x + 4$$

$$\begin{array}{l} +x \\ -x + y \end{array} < 4$$

$$y < x + 4$$

$$y \geq 0$$



PART 4:	Can Start		Can Partially		Can Do	
Can solve linear inequalities applications in context.						

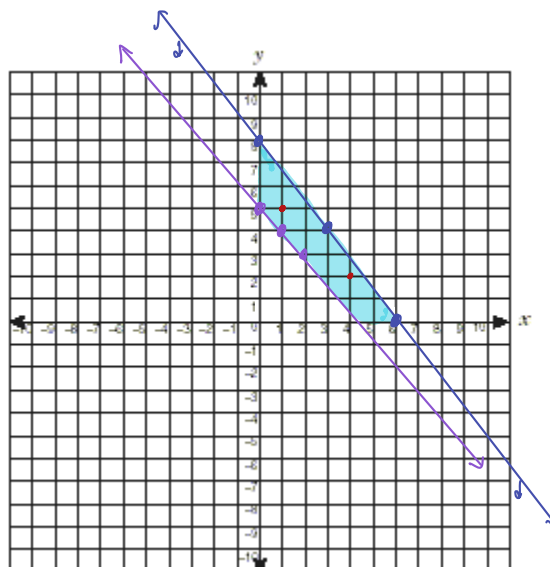
5) Scarlett can spend up to \$120 on souvenir T-shirts from the Olympics. She would like to buy at least 5 T-shirts to give to family and friends. The two styles of T-shirts cost \$20 or \$15 each. Create two linear inequalities, as well as two common sense restrictions, and graph the system (with shading). Then describe two possible ways for Scarlett to meet her requirements.

T-shirt style #1 = $x = \$20$ each $x \& y \geq 0$

T-shirt style #2 = $y = \$15$ each

Amount: $x + y \geq 5 \rightarrow y \geq -x + 5$

Money: $20x + 15y \leq 120$
 $\begin{array}{r} 20x + 15y \leq 120 \\ -20x \\ \hline 15y \leq -20x + 120 \\ \div 15 \\ \hline y \leq -\frac{4}{3}x + 8 \end{array}$



Two ways that Scarlett can meet the requirements:

Two possible scenarios (any of the shaded are good)

$(1, 5) \quad 20(1) + 15(5) \leq 120 \rightarrow 20 + 75 \leq 120$
 $95 \leq 120 \checkmark$

$(4, 2) \quad 20(4) + 15(2) \leq 120 \rightarrow 80 + 30 \leq 120$
 $110 \leq 120 \checkmark$

PART 5:	Can Start		Can Partially		Can Do	
Can optimize the solution to linear inequalities by creating an objective function.						

6) A farmer raises no more than 5000 of two types of chickens. It costs \$0.50 to raise the white chickens and \$0.75 to raise the brown chickens, and the total cost cannot exceed \$3000.

At the end of six weeks, a white chicken will weigh 3 pounds, and a brown chicken will weigh 4 pounds (**this info will be used to create your Objective Function**).

Create and graph a system of inequalities, and use it to find how many of each type of chicken should be raised to have the maximum number of pounds of chickens.

System of Equations:

Let B = brown chickens P = Pounds
 Let w = white chickens

Objective Function
 $P = 3w + 4B$

total
 chix $w + B \leq 5000$ $B \leq -w + 5000$

price $.5w + .75B \leq 3000$
 $(\frac{1}{2}w + \frac{3}{4}B \leq 3000) \times 4$

$2w + 3B \leq 12000$
 $-2w$ $-2w$
 $3B \leq -2w + 12000$
 3

$B \leq -\frac{2}{3}w + 4000$

Objective Function:

check: $(0, 0)$
 $(0, 4000)$
 $(3000, 2000)$
 $(5000, 0)$

objective function =

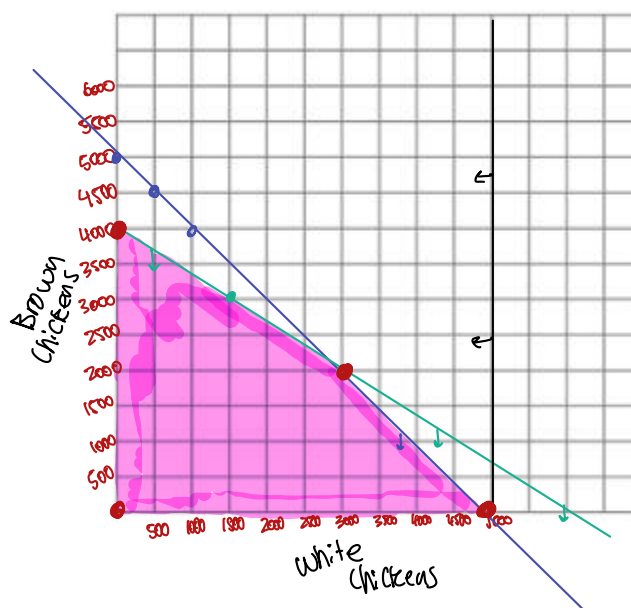
$P = 3w + 4B$

$P_{(0,0)} = 3(0) + 4(0) = 0$

$P_{(0,4000)} = 3(0) + 4(4000) = 16000$ lbs

$P_{(3000,2000)} = 3(3000) + 4(2000) = 17,000$ lbs \leftarrow max. value

$P_{(5000,0)} = 3(5000) + 4(0) = 15,000$ lbs



Final Answer: 3000 white & 4000 brown chickens
 w.s. yield a maximum amount of
 17,000 pounds.